

# Data-Driven Exploration of Climate Attractor Manifolds For Long-Term Predictability

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## Focal Area

This white paper responds to Focal Area 3. We seek to gain insight into decadal-scale climate predictability by applying novel manifold-finding probabilistic AI techniques to the complex data produced by Earth System models (ESMs) such as E3SM. The associated portfolio of research activities leverages DOE’s asset mix of HPC platforms, climate expertise, climate simulation codes, and AI expertise.

## Science Challenge

Climate and climate models are dynamical systems exhibiting properties that are interpretable through chaos theory. The theory contains an important concept that is relevant to multi-decade-scale climate prediction: a *chaotic attractor*. While the space containing all the possible states of the Earth’s atmosphere and ocean, the possible weather, is large, the realized states tend to stay near the smaller-dimensional attractor. This behavior is responsible for the “order behind the irregularity” [1] of climate phenomena. Climate change can be thought of as a change in the properties of the attractor, and predicting the climate over years to decades is equivalent to predicting how those properties will change. To date, the attractor has been a useful conceptual tool, but has not been amenable to direct characterization. A new development is the advent of efficient high-dimensional manifold-finding probabilistic AI techniques, which permit a data-driven characterization of the ESM attractor and its probability distribution over weather states. Such a characterization would result in a natural dimensional reduction — a “non-linear Principal Components Analysis (PCA) adapted to climate simulation data” — leading to important advances in scenario-based long-term climate prediction, long-term prediction of water cycle extremes, ESM verification, inter-model comparison, and process model development.

## Rationale

Climate prediction at multi-decade scales is an urgent priority in Earth System Science. Predictions of sea level and precipitation changes, and of average temperature rise due to greenhouse gas (GHG) emission scenarios, are attended by substantial modeling uncertainties [2]. Analysis of the causes of these discrepancies is challenging due the very complex and high-dimensional nature of ESM output. In order to reduce and better quantify the associated uncertainties we require new approaches to the interpretation of climate model output data. In particular, information-preserving dimension

reduction of such data is highly desirable. A promising approach to the required reduction is to seek a *data-driven representation of the dynamical attractor*.

In terms of chaos theory, an attractor is a finite-dimensional subspace in the infinite-dimensional space of possible climate states to which all real weather is confined. In the same language, the “invariant measure” on the attractor is the probability of each state’s occurrence. The promise that these ideas hold for climate simulation is that while simulation output consists of very high-dimensional data (all climate variables on an Earth surface-, ocean-, and atmosphere-spanning mesh), there is likely a much lower-dimensional surface embedded in this space to which all the states are confined. It would be well-worth locating and characterizing this manifold, since it would furnish a maximally-informative dimensional reduction of the simulation output — effectively a “non-linear PCA adapted to climate simulation data.” Analogously to PCA, this dimensional reduction could indicate clarifying and important features, correlations, covariances, and causalities.

Climate prediction is a qualitatively different enterprise from weather and seasonal/sub-seasonal forecasting: unlike such shorter-term forecasts, detailed current conditions have little bearing on decadal scale climate predictions and none at all on multi-decade scales, because memory of such conditions is progressively destroyed by chaotic dynamics on such timescales. Regions that are influenced by parts of the climate with a longer memory, such as the ocean, retain some specific predictability based on current conditions, but on multi-decade timescales even this memory is lost. Rather, we must seek to characterize how the distribution of weather states itself evolves under various forcing scenarios. The theoretical issue that underpins the problem of long-term climate prediction is summarized by the question *what is the structure of ESM attractors, and how does those attractors evolve under exogenous and random forcings?*

**The Opportunity:** The theoretical study of climate from the dynamical systems perspective is an active field with abundant literature [see, e.g 3, and references therein]. Nonetheless, the climate attractor has remained a rather abstract conception, useful for clarifying discussion but not amenable to explicit representation. With the advent of new probabilistic AI/ML manifold-finding methods and ever more powerful HPC resources, a new opportunity has arisen: *data-driven exploration of the climate attractor*. We can now deploy at scale computational AI models with expressive capacity comparable to the expected number of degrees of freedom associated with the attractor of a computational ESM, or that of a model subsystem. Using these AI models we expect enhanced predictability of ESMs in virtue of: (1) the capability to sample weather states from the resulting AI-based distribution, resulting in a novel kind of weather emulator, and in a new tool for the study of the statistics of water cycle extremes; (2) new information concerning what variables act together in important and possibly causal ways affecting climate prediction beyond seasonal scales; (3) new tools for the study of the differences between climate model outputs, and of the sensitivity of any climate model to its constituent process models; and (4) separate study of the attractors of climate *subsystems*, whether geographical (e.g. Tropical Pacific, Great Lakes) or variable projections (e.g. water vapor fluxes, stratospheric wind speeds), and of relations of such attractor structures to each other and to the properties of the models from which they arise.

## Narrative

AI/ML Approaches such as autoencoders [4] have proven adept at locating data submanifolds in high-dimensional spaces. Probabilistic variants — variational autoencoders (VA) [5], or variational information bottleneck (VIB) machines [6, 7, 8], possibly chained to powerful distribution-learning tools such as normalizing flows [9, 10] — can both find submanifold *and* approximate the data distribution on the submanifold. These methods can allow direct characterization of the structure

and evolution of dynamical attractors of ESMs and their subsystems.

Many approaches are feasible depending on the question to be answered, and the search for optimal approaches is an important research question. A “reference implementation” approach is to gather simulation output from ensembles of runs of a single model, and feed the complete data set, or a geographically-delimited dataset, or a physical subsystem dataset, to a probabilistic autoencoder-type manifold-learning AI code, such as a VIB system [6, 7, 8]. After training, the output is a low(er)-dimensional representation of the input data which may be directly queried for geometric and statistical properties, as well as sampled. We may, in this way, obtain compact weather state distributions that describe sea-surface temperature (SST) distributions, or tropical depression statistics.

**V&V:** Attractors may be very useful tools for studying sensitivities and GHG response differences between models. Inter-model comparison and reconciliation assisted by such studies could reduce spreads in decadal-scale scenario predictions, which are considerable at this time [2].

Model validation using data from weather stations, LIDAR, optical, UV and radar observations from ground-based and satellite platforms can play a key role in constraining attractor models, both through data assimilation-mediated process model parameter estimation and through direct application of observation operators to weather states sampled from the data-driven model. Examples of the latter are weather variable interpolations from model mesh boxes to station locations, or line-of-sight integration of optical signals across a model mesh. In this way the data-driven models can be compared to current and past observations, offering novel verification opportunities.

**Dynamical Theory:** Ideas from theoretical climate dynamics such as pull-back and stochastic attractor concepts [3] may be used to fashion attractor models to compare to the data-driven representation, or used to suggest specific analyses that extract information from that representation. Further fruitful interactions between dynamical theory and the data-driven attractor model may include linear resolvent analyses [11, 12], approachable through automatic differentiation of climate codes, or through proper orthogonal decomposition (POD) approaches [13].

**Subsystems:** Subsystem attractor analysis also makes possible the identification of key processes (or factors) of attractor geometry and state distribution. Noteworthy anomalies, such as those associated with tropical precipitation can be put under the microscope, to aid the search for variable interrelations associated with such anomalies. For example by exploring the importance of different factors, such as those associated to vegetation dynamics, production of volatile organic compounds (VOCs), and others, in driving precipitation events and other phenomena by analyzing their effects when they are included or not included in different models. This may also be a valuable approach for the study of anthropogenic effects due to land-use or agricultural policy.

**Impacts:** Decadal-scale prediction of climate can be closely coupled to the study of economic and social impacts. Climate change is already negatively impacting many economic sectors[14] including food production [15] as robust changes in the hydrology cycle [16, 17] impact rainfed agricultural in many regions around the world. Climate variability explains a large fraction of the historically variability in agricultural yields [18, 19] and the near-term changes in precipitation variability and extremes (which remain underrepresented in models[20]) need to be characterized to improve risk assessments to food production[21]. Improving understanding of expected climatological of the variability in the hydrological cycle including e.g. the El Niño Southern Oscillation (ENSO)[22], the Indian Ocean Dipole (IOD)[23], and the South Asian Monsoon more broadly [24] can therefore can directly lead to improved decadal-scale prediction of food and economic security. Other hydrology-related impact domains include infectious diseases [25], vector-borne diseases [26], flooding [27], hydropower [28], and wildfires [29].

## Suggested Partners/Experts

1. Michael Ghil and the [UCLA Theoretical Climate Dynamics Group](#).
2. Leonard Smith Virginia Tech.

## References

- [1] AA Tsonis and JB Elsner. Chaos, strange attractors, and weather. *Bulletin of the American Meteorological Society*, 70(1):14–23, 1989.
- [2] Rajendra K Pachauri, Myles R Allen, Vicente R Barros, John Broome, Wolfgang Cramer, Renate Christ, John A Church, Leon Clarke, Qin Dahe, Purnamita Dasgupta, et al. *Climate change 2014: synthesis report. Contribution of Working Groups I, II and III to the fifth assessment report of the Intergovernmental Panel on Climate Change*. Ipcc, 2014.
- [3] Michael Ghil and Valerio Lucarini. The physics of climate variability and climate change. *Rev. Mod. Phys.*, 92:035002, Jul 2020.
- [4] Ruslan Salakhutdinov. Nonlinear dimensionality reduction using neural networks. *RBM*, 2:1000, 2000.
- [5] Diederik P Kingma and Max Welling. Auto-encoding variational bayes. *arXiv preprint arXiv:1312.6114*, 2013.
- [6] Naftali Tishby, Fernando C Pereira, and William Bialek. The information bottleneck method. *arXiv preprint physics/0004057*, 2000.
- [7] Ohad Shamir, Sivan Sabato, and Naftali Tishby. Learning and generalization with the information bottleneck. *Theoretical Computer Science*, 411(29-30):2696–2711, 2010.
- [8] Alex Alemi, Ian Fischer, Josh Dillon, and Kevin Murphy. Deep variational information bottleneck. In *ICLR*, 2017.
- [9] Ivan Kobyzev, Simon Prince, and Marcus Brubaker. Normalizing flows: An introduction and review of current methods. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, page 1–1, 2020.
- [10] Sandeep Madireddy, Nan Li, Nesar Ramachandra, James Butler, Prasanna Balaprakash, Salman Habib, and Katrin Heitmann. A modular deep learning pipeline for galaxy-scale strong gravitational lens detection and modeling. *arXiv preprint arXiv:1911.03867*, 2019.
- [11] Benjamin Herrmann, Peter J Baddoo, Richard Semaan, Steven L Brunton, and Beverley J McKeon. Data-driven resolvent analysis. *arXiv preprint arXiv:2010.02181*, 2020.
- [12] Sean Symon, Denis Sipp, Peter J Schmid, and Beverley J McKeon. Mean and unsteady flow reconstruction using data-assimilation and resolvent analysis. *AIAA Journal*, 58(2):575–588, 2020.
- [13] Peer Nowack, Jakob Runge, Veronika Eyring, and Joanna D Haigh. Causal networks for climate model evaluation and constrained projections. *Nature communications*, 11(1):1–11, 2020.
- [14] Noah S. Diffenbaugh and Marshall Burke. Global warming has increased global economic inequality. *Proceedings of the National Academy of Sciences*, page 201816020, April 2019.
- [15] Deepak K. Ray, Paul C. West, Michael Clark, James S. Gerber, Alexander V. Prishchepov, and Snigdhanu Chatterjee. Climate change has likely already affected global food production. *PLOS ONE*, 14(5):e0217148, May 2019.

- [16] Maisa Rojas, Fabrice Lambert, Julian Ramirez-Villegas, and Andrew J. Challinor. Emergence of robust precipitation changes across crop production areas in the 21st century. *Proceedings of the National Academy of Sciences*, 116(14):6673–6678, April 2019.
- [17] Mariano S. Morales, Edward R. Cook, Jonathan Barichivich, Duncan A. Christie, Ricardo Villalba, Carlos LeQuesne, Ana M. Srur, M. Eugenia Ferrero, Álvaro González Reyes, Fleur Couvreur, Vladimir Matskovsky, Juan C. Aravena, Antonio Lara, Ignacio A. Mundo, Facundo Rojas, Mariã R. Prieto, Jason E. Smerdon, Lucas O. Bianchi, Mariano H. Masiokas, Rocio Urrutia-Jalabert, Milagros Rodriguez-Catón, Ariel A. Muñázoz, Moises Rojas-Badilla, Claudio Alvarez, Lidio Lopez, Brian H. Luckman, David Lister, Ian Harris, Philip D. Jones, A. Park Williams, Gonzalo Velazquez, Diego Aliste, Isabella Aguilera-Betti, Eugenia Marcotti, Felipe Flores, Tomãas Muñázoz, Emilio Cuq, and José. Boninsegna. Six hundred years of South American tree rings reveal an increase in severe hydroclimatic events since mid-20th century. *Proceedings of the National Academy of Sciences*, 117(29):16816–16823, July 2020.
- [18] Deepak K. Ray, James S. Gerber, Graham K. MacDonald, and Paul C. West. Climate variation explains a third of global crop yield variability. *Nature Communications*, 6(1):5989, May 2015.
- [19] Matias Heino, Michael J. Puma, Philip J. Ward, Dieter Gerten, Vera Heck, Stefan Siebert, and Matti Kummu. Two-thirds of global cropland area impacted by climate oscillations. *Nature Communications*, 9(1), December 2018.
- [20] Jacob Schewe, Simon N. Gosling, Christopher Reyer, Fang Zhao, Philippe Ciais, Joshua Elliott, Louis Francois, Veronika Huber, Heike K. Lotze, Sonia I. Seneviratne, Michelle T. H. van Vliet, Robert Vautard, Yoshihide Wada, Lutz Breuer, Matthias Bãšchner, David A. Carozza, Jinfeng Chang, Marta Coll, Delphine Deryng, Allard de Wit, Tyler D. Eddy, Christian Folberth, Katja Frieler, Andrew D. Friend, Dieter Gerten, Lukas Gudmundsson, Naota Hanasaki, Akihiko Ito, Nikolay Khabarov, Hyungjun Kim, Peter Lawrence, Catherine Morfopoulos, Christoph Mãšler, Hannes Müller Schmied, René Orth, Sebastian Ostberg, Yadu Pokhrel, Thomas A. M. Pugh, Gen Sakurai, Yusuke Satoh, Erwin Schmid, Tobias Stacke, Jeroen Steenbeek, Jörg Steinkamp, Qihong Tang, Hanqin Tian, Derek P. Tittensor, Jan Volkholz, Xuhui Wang, and Lila Warszawski. State-of-the-art global models underestimate impacts from climate extremes. *Nature Communications*, 10(1), December 2019.
- [21] Erik Chavez, Gordon Conway, Michael Ghil, and Marc Sadler. An end-to-end assessment of extreme weather impacts on food security. *Nature Climate Change*, 5(11):997–1001, November 2015.
- [22] James W Hansen, Alan W Hodges, and James W Jones. ENSO Influences on Agriculture in the Southeastern United States. *JOURNAL OF CLIMATE*, 11:8, 1998.
- [23] W. B. Anderson, R. Seager, W. Baethgen, M. Cane, and L. You. Synchronous crop failures and climate-forced production variability. *Science Advances*, 5(7):eaaw1976, July 2019.
- [24] Maximilian Auffhammer, V. Ramanathan, and Jeffrey R. Vincent. Climate change, the monsoon, and rice yield in India. *Climatic Change*, 111(2):411–424, March 2012.
- [25] David N. Fisman, Ashleigh R. Tuite, and Kevin A. Brown. Impact of El Niño Southern Oscillation on infectious disease hospitalization risk in the United States. *Proceedings of the National Academy of Sciences*, 113(51):14589–14594, December 2016.
- [26] Simon Hales, Phil Weinstein, Yvan Soares, and Alistair Woodward. El Niño and the Dynamics of Vectorborne Disease Transmission. *Environmental Health Perspectives*, 107(2):4, 1999.

- [27] Hossein Tabari. Climate change impact on flood and extreme precipitation increases with water availability. *Scientific Reports*, page 10, 2020.
- [28] Xingcai Liu, Qihong Tang, Nathalie Voisin, and Huijuan Cui. Projected impacts of climate change on hydropower potential in China. *Hydrol. Earth Syst. Sci.*, page 17, 2016.
- [29] John T. Abatzoglou and A. Park Williams. Impact of anthropogenic climate change on wildfire across western US forests. *Proceedings of the National Academy of Sciences*, 113(42):11770–11775, October 2016.